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## ANALYSIS OF VOLTAGE AND FREQUENCY CONTROL IN ISLANDED MICROGRID FED BLDC MOTOR DRIVE

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**Abstract:** Micro grids being a new developing technology operate in two distinct modes of operation, namely, the utility-grid-connected mode and the autonomous (or islanded) mode. In transition from the utility-grid-connected mode to the autonomous mode, the frequency of a micro grid can be seriously affected due to unbalance between power generation and power demand and at that moment, micro-sources may respond slowly to eliminate this unbalancing situation. To solve this interruption and to operate the micro grid steadily, some rapid response storage systems, namely Energy Storage Systems (ESSs) are needed. The stability is an important topic to plan and manage the energy in the microgrids as the same as the conventional power systems. The voltage and frequency stability is one of the most important issues recently studied in microgrids. The objectives of this paper are the modelling and designing of the components and optimal controllers for the voltage and frequency control of the AC/DC microgrid under the different disturbances. Without using any controller, an increment in active and reactive power leads to frequency and voltage drop respectively. Therefore, droop controllers are essential in MGs. In this paper, a microgrid has been modeled and its voltage and frequency behavior in presence of BLDC motor drive characteristics has been analyzed.

**Key Words:** Energy storage system (ESS), microgrid (MG), P/Q droop, small-signal model, V/f droop, BLDC Motor.

### I. INTRODUCTION

Nowadays most of electrical power is generated by the centralized power plants usually including large water turbines, fossil fuel combustion engines or nuclear reactors. Then, the generated power is transferred to the load centers through the most economic and effective way by the transmission lines. The centralized power generation has been used for several decades. However, there are defects in such systems, the reliability and power supply availability are the most important among them and also the long transmission lines make huge

economic losses. Furthermore, given the fact that the infrastructure of the many power systems, has been used for a long time and their life is often the end, therefore they may not response to increasing electrical power requirements and their maintenance needs large financial budgets. As a result, the current power systems are usually operated around their full capacity. A blackout occurred in north east USA on August 2003 due to the overload made in a main transmission area, is a typical example for the above problems. Also, in many cases, from

an environmental perspective, the construction of a new large-scale power plant may not be the suitable option and even if construction is decided, selection and preparation of its location will be introduced as real challenges. To solve these inevitable problems of the concentrated power systems, application of distributed generation (DG) units in distribution systems can be considered as one of several practical and effective solutions. This application will lead to the emergence of smaller distribution networks, called microgrids [1]. In general, a microgrid is a collection of micro sources and loads often providing both electricity and heat to the local area [2]. In a microgrid, a customary requirement is installing an energy storage system. In this paper, the focus will be on the control voltage of the microgrid and frequency control will be considered as one of the constraints on the problem. Design and modeling of controllers are done to control the loads bus voltage. Small disturbances (such as changes in power of the loads and generators) and large disturbances (such as a short circuit occurring on the network and transient state between two parallel and islanded operation modes) are considered to study the voltage stability of the proposed microgrid.

## II. CONTROL OF MPS FOR AUTONOMOUS MG

As discussed above, the operation of an autonomous MG is usually more complex than grid-connected one since it cannot always have synchronous generators in a small and customized system. How to establish and maintain system frequency and voltage, i.e., the choice and control of MPS, is a problem in this situation. ESS with converter can be controlled flexibly with different output characteristics and

is considered as a potential MPS for MG autonomous operation [21]. There are usually two typical methods that can be adopted to control ESS as a MPS, including V/f control and droop control. Due to good current sharing effect, this paper focuses on droop control. Traditional droop control named in this paper as VFDC is analyzed and compared with the proposed hybrid VFDC/PQDC.

### a) VFDC

VFDC-based ESS mimics the characteristics of traditional synchronous machine with voltage angle and amplitude regulated according to its output active power and reactive power. The equivalent circuit of a MG with VFDC-based ESSs can be illustrated in Fig.1, where the two ESSs are equivalent as voltage sources  $U_1 \angle \varphi_1$  and  $U_2 \angle \varphi_2$ , respectively.

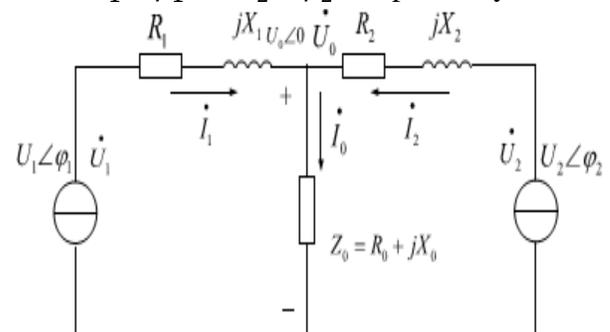


Fig.1. MG equivalent circuit based on VFDC method

The load voltage is derived from Fig.2 as

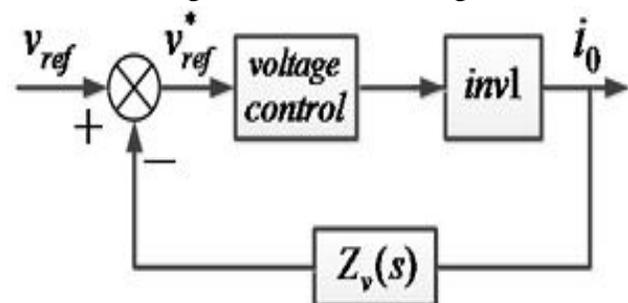


Fig.2 Schematic of virtual impedance control loop

$$\dot{U}_0 = \frac{\frac{\dot{U}_1}{Z_1} + \frac{\dot{U}_2}{Z_2}}{\frac{1}{Z_0} + \frac{1}{Z_1} + \frac{1}{Z_2}} \quad (1)$$

Where  $Z_1 = R_1 + jX_1$  and  $Z_2 = R_2 + jX_2$  are equivalent line impedance of  $U_1 \angle \varphi_1$  and  $U_2 \angle \varphi_2$ , respectively. The output current of the two voltage sources can be derived

$$\dot{I}_1 = \frac{\dot{U}_1 - \dot{U}_0}{Z_1} = \frac{(Z_2 + Z_0)\dot{U}_1 - Z_0\dot{U}_2}{Z_1Z_2 + Z_0Z_2 + Z_1Z_0} \quad (2)$$

$$\dot{I}_2 = \frac{\dot{U}_2 - \dot{U}_0}{Z_2} = \frac{(Z_1 + Z_0)\dot{U}_2 - Z_0\dot{U}_1}{Z_1Z_2 + Z_0Z_2 + Z_1Z_0} \quad (3)$$

The apparent power of the two ESSs

$$\dot{S}_1 = \dot{U}_1 \times \dot{I}_1^* = \dot{U}_1 \times \frac{(Z_2^* + Z_0^*)\dot{U}_1^* - Z_0^*\dot{U}_2^*}{Z_1^*Z_2^* + Z_0^*Z_2^* + Z_1^*Z_0^*} \quad (4)$$

$$\dot{S}_2 = \dot{U}_2 \times \dot{I}_2^* = \dot{U}_2 \times \frac{(Z_1^* + Z_0^*)\dot{U}_2^* - Z_0^*\dot{U}_1^*}{Z_1^*Z_2^* + Z_0^*Z_2^* + Z_1^*Z_0^*} \quad (5)$$

Where the superscript \* is the corresponding conjugate phasors. It can be seen from (2) to (5) that, the output current and apparent power of the two ESSs are dependent to the value of  $\dot{U}_1$  and  $\dot{U}_2$ , as well line parameters of  $Z_1$  and  $Z_2$ . As a result, the current sharing of ESSs can only be implemented by the coordinated control of  $\dot{U}_1$  and  $\dot{U}_2$  provided that line parameters  $Z_1$  and  $Z_2$  are given.

$$\frac{(Z_2 + Z_0)\dot{U}_1 - Z_0\dot{U}_2}{Z_1Z_2 + Z_0Z_2 + Z_1Z_0} = \frac{(Z_1 + Z_0)\dot{U}_2 - Z_0\dot{U}_1}{Z_1Z_2 + Z_0Z_2 + Z_1Z_0} \quad (6)$$

The phase angle difference of  $\dot{U}_1$  and  $\dot{U}_2$  can be derived by multiplication of  $\dot{U}_2^*$  to both sides of (6)

$$\angle(\varphi_2 - \varphi_1) = \frac{U_2 \angle 2Z_0 + Z_1}{U_1 \angle 2Z_0 + Z_2} \quad (7)$$

Where  $\varphi_1$  and  $\varphi_2$ ,  $U_1$  and  $U_2$  are the phase angle and voltage amplitude of  $\dot{U}_1$  and  $\dot{U}_2$ , respectively.

$$\begin{aligned} \cos(\varphi_1 - \varphi_2) &= \frac{U_2(2R_0 + R_1)(2R_0 + R_2) + (2X_0 + X_1)(2X_0 + X_2)}{U_1((2R_0 + R_2)^2 + (2X_0 + X_2)^2)} \end{aligned} \quad (8)$$

$$\begin{aligned} \sin(\varphi_1 - \varphi_2) &= \frac{U_2(2X_0 + X_1)(2R_0 + R_2) - (2R_0 + R_1)(2X_0 + X_2)}{U_1((2R_0 + R_2)^2 + (2X_0 + X_2)^2)} \end{aligned} \quad (9)$$

From (8) and (9), it can be seen that the power distribution in the system is easily affected by line impedances. This complex the control of ESS and decreases the current sharing effect due to the uncertainty of line parameters.

## b) Hybrid VFDC/PQDC

PQDC-based ESS regulates its output active power and reactive power according to MG frequency and voltage deviations from their nominal values. In Fig.1, provided that ESS  $U_2$  is controlled with PQDC, the equivalent circuit can be described as a connection of voltage source  $U_1 \angle \varphi_1$  and current source  $I_2 \angle \varphi_2$ .

According to Kirchhoff voltage and current theory, the output current of the VFDC-based voltage source  $U_1 \angle \varphi_1$  is

$$\dot{I}_1 = \frac{\dot{U}_1 - \dot{I}_2 Z_0}{Z_0 + Z_1} \quad (10)$$

Its apparent power can be derived as

$$\dot{S}_1 = \dot{U}_1 \dot{I}_1^* = \dot{U}_1 \left( \frac{\dot{U}_1 - \dot{I}_2 Z_0}{Z_0 + Z_1} \right)^* = \frac{U_1^2 - \dot{U}_1 \dot{I}_2^* Z_0^*}{Z_0^* + Z_1^*} \quad (11)$$

It can be seen that  $\dot{S}_1$  is independent of  $Z_2$ . If  $\dot{U}_1$  and line parameters are given,  $\dot{S}_1$  is determined only by the value of  $\dot{I}_2$ . Therefore,

$\dot{S}_1$  and  $\dot{I}_1$  can be regulated through the control of  $\dot{I}_2$ . As a result, the diversity and uncertainty of line parameters of  $Z_1$  and  $Z_2$  have no impact on MG power control. This means that the hybrid VFDC/PQDC system is better in current sharing control than the VFDC system. Though the above MG autonomous operation control scheme is ESSs-based, it is suitable for other converter based dispatchable micro resources such as single-shaft micro-turbine and fuel cell. This paper takes ESSs as example to make the analysis simple.

### III. PROPOSED HYBRID VFDC/PQ DC CONTROL SCHEME

Based on the above analysis, a novel MG control method is proposed in this paper based on hybrid VFDC/PQDC. The VFDC-based ESS is controlled as a V/f droop voltage source with output voltage and frequency determined by its active power and reactive power. While the PQDC-based ESS is controlled as a P/Q source with output active power and reactive power determined by the voltage and frequency deviations on its output terminal. To decouple the active power and reactive power due to the resistive line parameters, virtual impedance control is adopted.

#### a) Virtual Impedance Control

According to, the active and reactive power allocation of two converters with a common bus can be expressed as

$$P = \left( \frac{EV}{Z} \cos \phi - \frac{V^2}{Z} \right) \cos \theta + \frac{EV}{Z} \sin \phi \sin \theta \quad (12)$$

$$Q = \left( \frac{EV}{Z} \cos \phi - \frac{V^2}{Z} \right) \sin \theta - \frac{EV}{Z} \sin \phi \cos \theta \quad (13)$$

Where  $E$  and  $V$  are the amplitudes of converters output voltage and bus voltage,  $\phi$  is the power angle,  $Z$  and  $\theta$  are the magnitude and the phase of output impedance. For high-voltage

transmission system, it can be assumed that the line impedance is predominant inductive ( $\theta = 90^\circ$ ). Then, (12) and (13) can be simplified as

$$P = \frac{EV}{X} \sin \phi, \quad Q = \frac{EV \cos \phi - V^2}{X} \quad (14)$$

Where  $X$  is line reactance

While for low-voltage distribution system with resistive impedance ( $\theta = 0^\circ$ ), (12) and (13) can be simplified as

$$P = \frac{EV \cos \phi - V^2}{R}, \quad Q = -\frac{EV}{R} \sin \phi \quad (15)$$

Where  $R$  is line resistance

As can be seen from (14) and (15), line impedance affects the rule of active and reactive power distribution between converters. Since the  $P-f$  and  $Q-v$  decoupling of traditional droop control is based on inductive impedance, the control of low/medium voltage MG with resistive impedance should be adjusted. Virtual impedance control is one of the potential methods, which control converter output impedance to be inductive and then the total impedance inductive. Fig.2 shows the schematic of the virtual impedance control loop, where  $Z_v(s)$  is the virtual impedance equivalent as an inductor  $L_v$ . It is in fact a voltage correction, as shown in Fig.3, where  $v_{ref}$  is the reference voltage,  $v_{ref}^*$  is that after modification,  $i_0$  the output current, and  $i_0 \omega L_v$  the voltage drop on virtual inductor  $L_v$ .

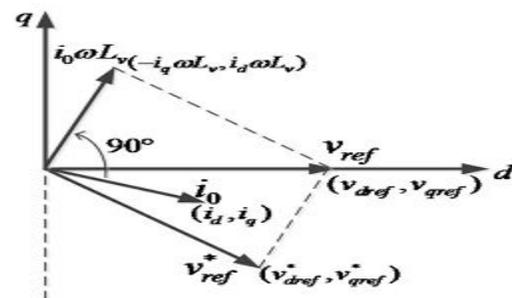


Fig.3. Phasor diagram of virtual impedance control based on  $d-q$  axis

The reference output voltage can be obtained

$$\begin{aligned} v_{dref}^* &= v_{dref} + i_q \omega L_v \\ v_{qref}^* &= v_{qref} - i_d \omega L_v \end{aligned} \quad (16)$$

As a result, the equivalent impedance is controlled to be inductive which enables  $P$ - $f$  and  $Q$ - $v$  decoupling. Moreover, the active and reactive current sharing among the parallel connected ESSs can be improved since their output impedances are definite.

### b) VFDC Control

The VFDC-based ESS is controlled to output certain frequency and voltage according to its active and reactive power. Since the virtual inductor  $L_v$  will absorb certain reactive power  $Q_v$ , it is taken as a correction to the reactive power reference  $Q^*$ . The droop control loop with reactive power compensation is illustrated in Fig.4.

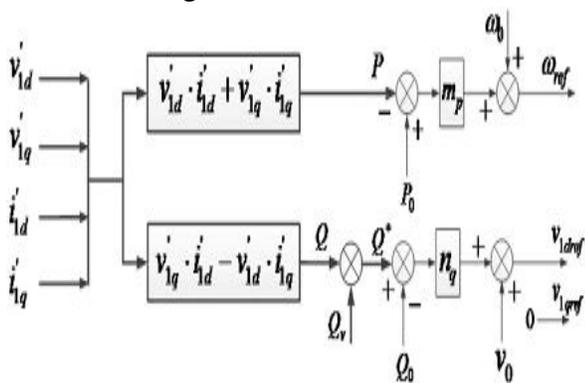


Fig.4. VFDC control loop with reactive power compensation

Therefore, the reference frequency  $\omega_{ref}$  and voltage  $v_{ref}$  of VFDC converter can be written as

$$\begin{aligned} \omega_{ref} &= \omega_0 + m_p \cdot (P_0 - P) \\ v_{ref} &= v_0 + n_q \cdot (Q_0^* - Q) \end{aligned} \quad (17)$$

Where  $P_0$  and  $Q_0$  are the rated active and reactive power,  $P$  and  $Q$  are the actual active and reactive power output,  $m_p$  and  $n_q$  are the droop coefficient of active and reactive power

for VFDC,  $\omega_0$  and  $v_0$  are the nominal frequency and voltage, respectively. With the reference frequency  $\omega_{ref}$  and voltage  $v_{ref}$  determined, the VFDC-based converter control can be implemented with the virtual impedance loop, voltage loop, and current loop shown in Fig.5.

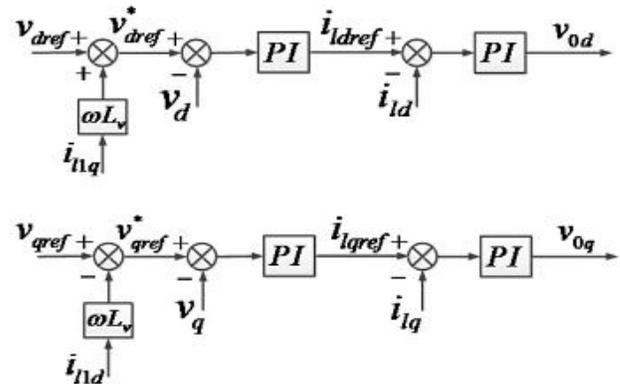


Fig.5. Virtual impedance loop, voltage loop, and current loop of VFDC ( $i_{ld}^* \omega L_v$  and  $i_{lq}^* \omega L_v$  denote the virtual impedance loop, respectively)

### c) PQDC Control

The PQDC-based ESS is controlled to provide certain active power and reactive power according to system frequency and local voltage deviations from their nominal values. Similarly, due to the voltage drop on virtual inductor  $L_v$ , the reference voltage  $v^*$  is corrected with a virtual inductor voltage  $v_v$  in the droop control loop, as shown in Fig.6.

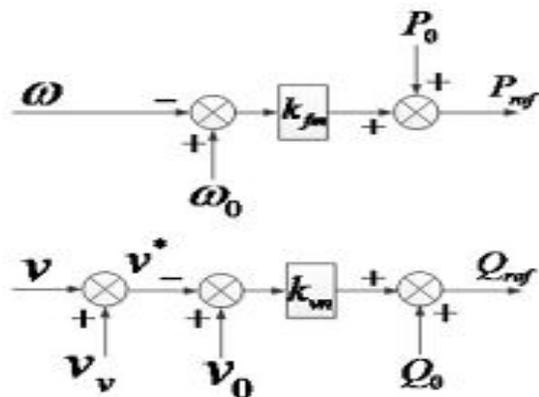


Fig.6. PQDC control loop with voltage correction

Therefore, the reference active and reactive power of PQ DC converter can be written as

$$\begin{aligned} P_{ref} &= P_0 + k_{fm}(\omega_0 - \omega) \\ Q_{ref} &= Q_0 + k_{vn}(v_0 - v^*) \end{aligned} \quad (18)$$

Where  $k_{fm}$  and  $k_{vn}$  are the droop coefficient of frequency and voltage for PQDC. With the reference active power  $P_{ref}$  and reactive power  $Q_{ref}$  determined, the PQDC converter control can be implemented with the virtual impedance loop, voltage loop, and current loop as shown in Figs 7 and 8, respectively.

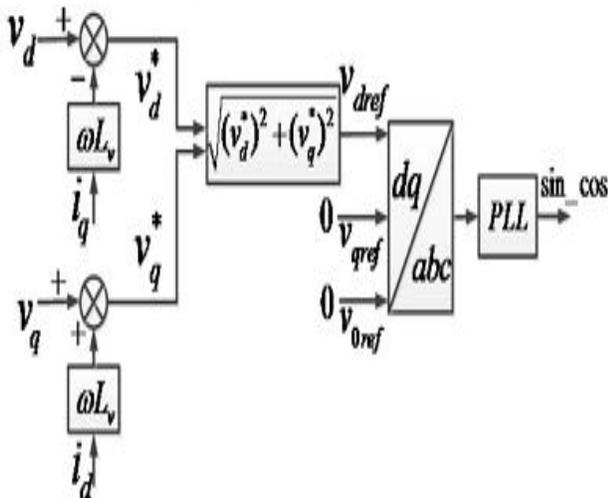


Fig.7. Virtual impedance loop of PQDC

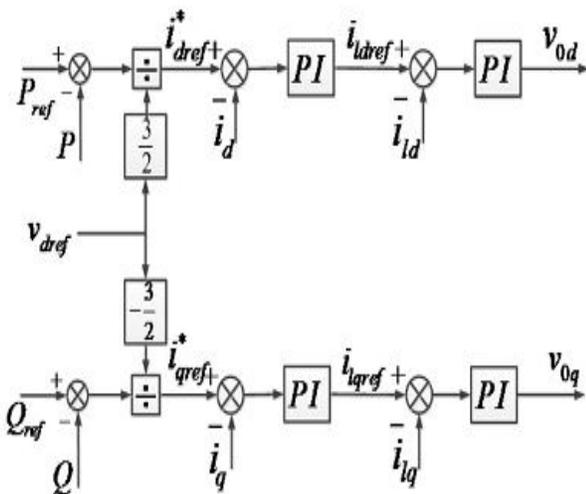


Fig.8. Voltage and current loop of PQDC

## IV. SMALL-SIGNAL MODEL AND ANALYSIS

The equivalent circuit of an ESSs-based autonomous MG can be illustrated in Fig.9. The VFDC-based ESS and PQDC-based ESS connected to load ( $R_3, L_3, C_p$ ) through line impedance of ( $R_1, L_1$ ) and ( $R_2, L_2$ ), respectively. ( $R_4, L_4$ ), and ( $R_5, L_5$ ) are their local loads, which can be omitted to simplify the analysis process.

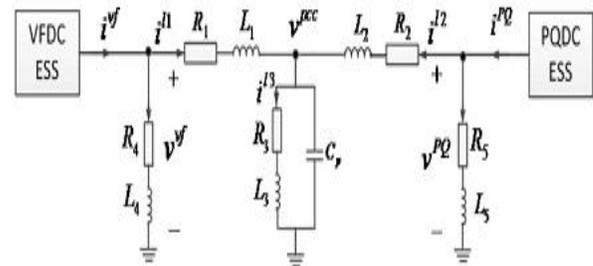


Fig.9 Equivalent circuit of ESSs-based autonomous MG

Both of the VFDC-based ESS and PQDC-based ESS is composed of a three-leg converter, LC filter, and grid coupling inductor. Fig.10 shows the diagram of ESS converter where  $L_{fm}$ ,  $C_{fm}$ , and  $r_{fm}$  are filter inductor, capacitor, and equivalent resistor, respectively.  $L_{cm}$  and  $r_{cm}$  are grid coupling inductor and its equivalent resistance. The subscript denotes the type of ESS with  $m=1$  as the VFDC controlled ESS,  $m=2$  as the PQDC one.

### a) State-Space Model of VFDC-Based ESS

For VFDC-based ESS, the following equations can be derived from Fig.10:

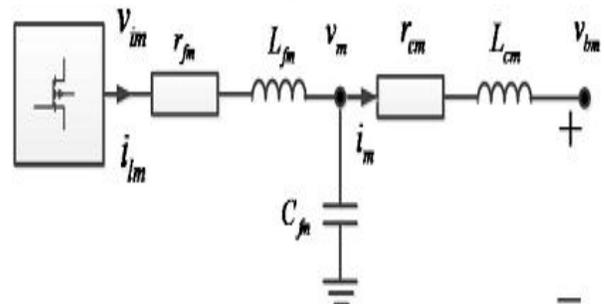


Fig.10. Equivalent circuit of the ESS converter

$$\begin{aligned}
 v_{i1} - v_1 &= i_{l1} \cdot r_{f1} + L_{f1} \cdot \frac{di_{l1}}{dt} \\
 v_1 - v_{b1} &= r_{c1} i_{l1} + L_{c1} \cdot \frac{di_1}{dt} \\
 C_{f1} \cdot \frac{dv_1}{dt} &= i_{l1} - i_1.
 \end{aligned} \tag{19}$$

The small-signal model of the power circuit of ESS in its rotary reference frame can be expressed as

$$\dot{\Delta x}_1 = A_1 \Delta x_1 + B_1 \Delta v_{i1} + B_2 \Delta \omega_1 + B_3 \Delta v_{b1} \tag{20}$$

$$\Delta x_1 = [\Delta i_{l1d} \ \Delta i_{l1q} \ \Delta i_{1d} \ \Delta i_{1q} \ \Delta v_{1d} \ \Delta v_{1q}]$$

$$\Delta v_{i1} = [\Delta v_{i1d} \ \Delta v_{i1q}]$$

$$\Delta v_{b1} = [\Delta v_{b1d} \ \Delta v_{b1q}].$$

$(\Delta i_{l1d} \ \Delta i_{l1q})$ ,  $(\Delta i_{1d} \ \Delta i_{1q})$ , and  $(\Delta v_{1d} \ \Delta v_{1q})$  are filter inductor current, converter output current, and filter capacitor voltage in  $d_1-q_1$  reference frame,  $(\Delta v_{i1d} \ \Delta v_{i1q})$  and  $(\Delta v_{b1d} \ \Delta v_{b1q})$  filter inductor voltage and bus voltage in  $d_1-q_1$  reference frame.  $\omega_1$  is the relative velocity of  $d_1-q_1$  to the global rotary reference frame. According to VFDC shown in Fig.4 and (17), the increment of active power and reactive power can be derived as (21) given that  $v_{1dref} = v_{ref}$  and  $v_{1qref} = 0$

$$\begin{aligned}
 \Delta P &= \Delta v'_{1d} \cdot i_{1d}^0 + \Delta v'_{1d} \cdot \Delta i'_{1d} + \Delta v'_{1q} \cdot \Delta i'_{1q} + \Delta v'_{1q} \cdot i_{1q}^0 \\
 \Delta Q &= \Delta v'_{1d} \cdot i_{1q}^0 + \Delta v'_{1d} \cdot \Delta i'_{1q} - v_{1q}^0 \cdot \Delta i'_{1d} - \Delta v'_{1q} \cdot i_{1d}^0
 \end{aligned} \tag{21}$$

Where  $\Delta v'_{1d}, \Delta v'_{1q}, \Delta i'_{1d}, \Delta i'_{1q}$  are the filtered values of  $\Delta v_{1d}, \Delta v_{1q}, \Delta i_{1d}, \Delta i_{1q}, v_{1d}^0, v_{1q}^0, i_{1d}^0, i_{1q}^0$  the steady-state value of  $\Delta v'_{1d}, \Delta v'_{1q}, \Delta i'_{1d}, \Delta i'_{1q}$ , respectively. The control process of VFDC-based ESS shown in Fig.3.5 can be illustrated in detail in Fig.11.

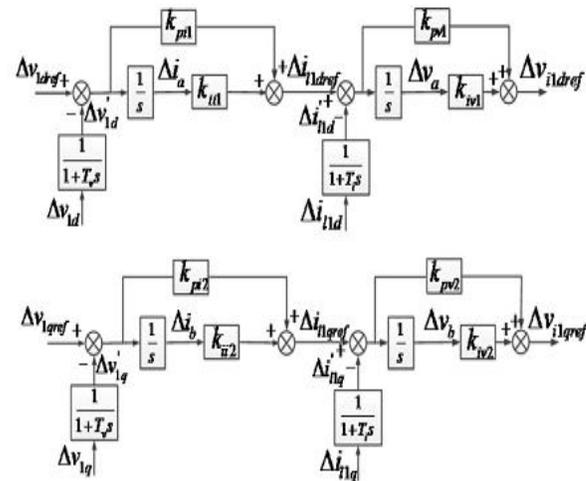


Fig.11. Voltage loop and current loop of VFDC

The filter parameters should meet the requirements

$$\begin{aligned}
 \frac{d\Delta i'_{1d}}{dt} &= \frac{1}{T_i} \Delta i_{1d} - \frac{1}{T_i} \Delta i'_{1d} \\
 \frac{d\Delta i'_{1q}}{dt} &= \frac{1}{T_i} \Delta i_{1q} - \frac{1}{T_i} \Delta i'_{1q} \\
 \frac{d\Delta v'_{1q}}{dt} &= \frac{1}{T_v} \Delta v_{1q} - \frac{1}{T_v} \Delta v'_{1q} \\
 \frac{d\Delta v'_{1d}}{dt} &= \frac{1}{T_v} \Delta v_{1d} - \frac{1}{T_v} \Delta v'_{1d} \\
 \frac{d\Delta i'_{1q}}{dt} &= \frac{1}{T_i} \Delta i_{1q} - \frac{1}{T_i} \Delta i'_{1q} \\
 \frac{d\Delta i'_{1d}}{dt} &= \frac{1}{T_i} \Delta i_{1d} - \frac{1}{T_i} \Delta i'_{1d}
 \end{aligned} \tag{22}$$

Where  $\Delta i'_{1d}$  and  $\Delta i'_{1q}$  are the filtered values of  $\Delta i_{1d}$  and  $\Delta i_{1q}$ , respectively. Therefore, the small-signal model of VFDC based ESS can be written as

$$\dot{x}_{c1} = A_{c11} \Delta x_{c1} + A_{c12} \Delta x_1 + A_{c13} [\Delta v_{1ref}, \Delta \omega_{1ref}] \tag{23}$$

Where

$\Delta x_{c1} = [\Delta i'_{1d}, \Delta i'_{1q}, \Delta v'_{1d}, \Delta v'_{1q}, \Delta i_a, \Delta v_a, \Delta i_b, \Delta v_b, \Delta \omega_1]$  with  $\Delta i_a, \Delta v_a, \Delta i_b, \Delta v_b$  as control variables. Taking the reference values of  $\Delta v_{1dref}$  and  $\Delta v_{1qref}$  being tracked, the following equation can be obtained.

$$\Delta v_{i1} = D_{11} \Delta x_{c1} + D_{12} [\Delta v_{1ref} \ \Delta \omega_{1ref}] \tag{24}$$

Where

$$D_{11} = \begin{bmatrix} -k_{pv1} & 0 & i_{1q}^{\circ} k_{pv1} k_{pi1} n_q & -i_{1d}^{\circ} k_{pv1} k_{pi1} n_q & -k_{pi1} k_{pv1} \\ 0 & -k_{pv2} & 0 & 0 & 0 \\ -v_{1d}^{\circ} k_{pv1} k_{pi1} n_q & k_{ii1} k_{pv1} & k_{iv1} & 0 & 0 & 0 \\ -k_{pi2} k_{pv2} & 0 & 0 & k_{ii2} k_{pv2} & k_{iv2} & 0 \end{bmatrix}$$

$$D_{12} = \begin{bmatrix} k_{pv1} k_{pi1} & 0 \\ 0 & 0 \end{bmatrix}$$

Combining (17) and (21)

$$\Delta\omega_1 = E_{11} \Delta x_{c1} + E_{12} [\Delta v_{1ref}, \Delta\omega_{1ref}] \quad (25)$$

Where

$$E_{11} = \begin{bmatrix} 0 & 0 & -m_p v_{1d}^{\circ} & -m_p v_{1q}^{\circ} & -m_p i_{1d}^{\circ} & -m_p i_{1q}^{\circ} & 0 & 0 & 0 & 0 \end{bmatrix}$$

$$E_{12} = \begin{bmatrix} 0 & 1 \end{bmatrix}$$

Then, (20) can be rewritten as

$$\dot{\Delta x}_1 = A A_1 \Delta x_1 + A B_1 \Delta x_{c1} + B B_1 [\Delta v_{1ref}, \Delta\omega_{1ref}] + B_3 \Delta v_{b1} \quad (26)$$

## b) State-Space Model of PQDC-Based ESS

According to Fig.10 and (19), it can be obtained

$$\dot{\Delta x}_2 = A_2 \Delta x_2 + B_1' \Delta v_{i2} + B_2' \Delta\omega_2 + B_3' \Delta v_{b2} \quad (27)$$

Where

$$\Delta x_2 = \begin{bmatrix} \Delta i_{i2d} & \Delta i_{i2q} & \Delta i_{2d} & \Delta i_{2q} & \Delta v_{2d} & \Delta v_{2q} \end{bmatrix}$$

$$\Delta v_{i2} = \begin{bmatrix} \Delta v_{i2d} & \Delta v_{i2q} \end{bmatrix}$$

$$\Delta v_{b2} = \begin{bmatrix} \Delta v_{b2d} & \Delta v_{b2q} \end{bmatrix}$$

$(\Delta i_{i2d}, \Delta i_{i2q})$ ,  $(\Delta i_{2d}, \Delta i_{2q})$ , and  $(\Delta v_{2d}, \Delta v_{2q})$  are filter inductor current, converter output current, and filter capacitor voltage in  $d_2$ - $q_2$  reference frame,  $(\Delta v_{i2d}, \Delta v_{i2q})$  and  $(\Delta v_{b2d}, \Delta v_{b2q})$  filter inductor voltage and bus voltage.  $\omega_2$  is the relative velocity of  $d_2$ - $q_2$  to the global  $d$ - $q$  reference frame.

According to PQDC control shown in Fig.3.6 and (18), the increment of active power and reactive power can be derived

$$\Delta P = \Delta v_{2d}' \cdot i_{2d}^{\circ} + v_{2d}^{\circ} \cdot \Delta i_{2d}' + v_{2q}^{\circ} \cdot \Delta i_{2q}' + \Delta v_{2q}' \cdot i_{2q}^{\circ}$$

$$\Delta Q = \Delta v_{2d}' \cdot i_{2q}^{\circ} + v_{2d}^{\circ} \cdot \Delta i_{2q}' - v_{2q}^{\circ} \cdot \Delta i_{2d}' - \Delta v_{2q}' \cdot i_{2d}^{\circ} \quad (28)$$

Where  $\Delta v_{2d}', \Delta v_{2q}', \Delta i_{2d}', \Delta i_{2q}'$  are the filtered values of  $\Delta v_{2d}, \Delta v_{2q}, \Delta i_{2d}, \Delta i_{2q}, v_{2d}^{\circ}, v_{2q}^{\circ}, i_{2d}^{\circ}, i_{2q}^{\circ}$  the steady-state values of  $\Delta v_{2d}', \Delta v_{2q}', \Delta i_{2d}', \Delta i_{2q}'$ , respectively. The detailed control process of VFDC-based ESS is shown in Fig.12 with phase lock loop (PLL) illustrated in Fig.13. The actual active power and reactive power can be calculated

$$P = v_{2d}' \cdot i_{2d}' + v_{2q}' \cdot i_{2q}'$$

$$Q = v_{2d}' \cdot i_{2q}' - v_{2q}' \cdot i_{2d}' \quad (29)$$

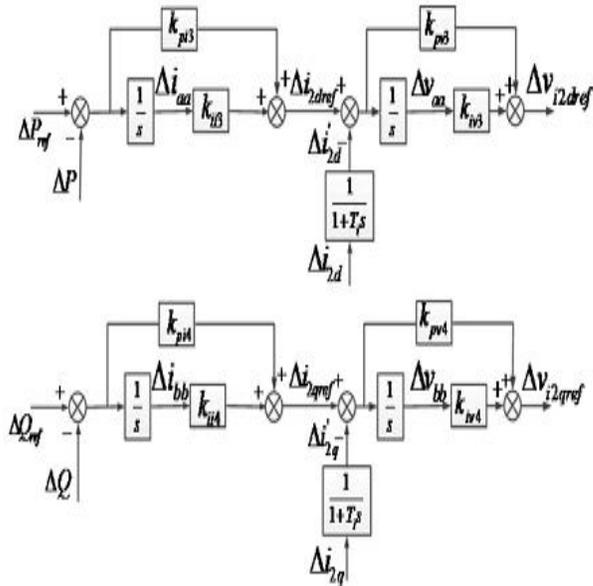


Fig.12. Voltage loop and current loop of PQDC

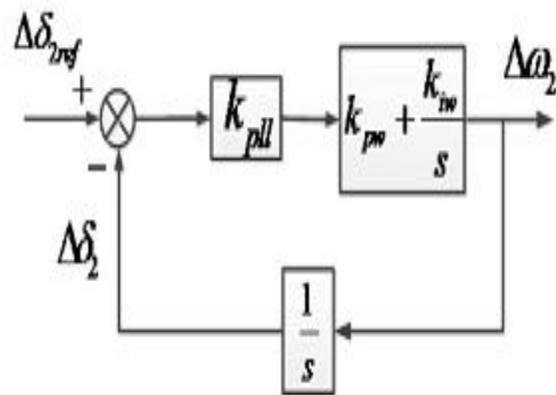


Fig.13. PLL of PQDC

From Fig.13, it can be derived that

$$\begin{aligned} [\Delta\delta_2] &= \frac{v_{2d}^o}{(v_{2d}^o)^2 + (v_{2q}^o)^2} \Delta v'_{2q} - \frac{v_{2q}^o}{(v_{2d}^o)^2 + (v_{2q}^o)^2} \Delta v'_{2d} \\ &= \begin{bmatrix} 0 & 0 & 0 & 0 & -\frac{v_{2q}^o}{(v_{2d}^o)^2 + (v_{2q}^o)^2} & \frac{v_{2d}^o}{(v_{2d}^o)^2 + (v_{2q}^o)^2} & 0 & 0 & 0 & 0 \end{bmatrix} \Delta x_{c2}. \end{aligned} \quad (30)$$

The above voltages should meet the following requirement:

$$\Delta v = \Delta v'_{2d} \cdot \frac{v_{2d}^o}{v^o} + \Delta v'_{2q} \cdot \frac{v_{2q}^o}{v^o} \quad (31)$$

Where

$$v^o = \sqrt{(v_{2d}^o)^2 + (v_{2q}^o)^2}.$$

The filter parameters should meet the requirements

$$\begin{aligned} \frac{d\Delta i'_{12d}}{dt} &= \frac{1}{T_i} \Delta i_{12d} - \frac{1}{T_i} \Delta i'_{12d} \\ \frac{d\Delta i'_{12q}}{dt} &= \frac{1}{T_i} \Delta i_{12q} - \frac{1}{T_i} \Delta i'_{12q} \\ \frac{d\Delta v'_{2q}}{dt} &= \frac{1}{T_v} \Delta v_{2q} - \frac{1}{T_v} \Delta v'_{2q} \\ \frac{d\Delta v'_{2d}}{dt} &= \frac{1}{T_v} \Delta v_{2d} - \frac{1}{T_v} \Delta v'_{2d} \\ \frac{d\Delta i'_{2q}}{dt} &= \frac{1}{T_i} \Delta i_{2q} - \frac{1}{T_i} \Delta i'_{2q} \\ \frac{d\Delta i'_{2d}}{dt} &= \frac{1}{T_i} \Delta i_{2d} - \frac{1}{T_i} \Delta i'_{2d} \end{aligned} \quad (32)$$

Where  $\Delta i'_{12d}$  and  $\Delta i'_{12q}$  are the filtered value of  $\Delta i_{12d}$  and  $\Delta i_{12q}$  respectively. Combining the above equation, we can get

$$\dot{x}_{c2} = A_{c21} \Delta x_{c2} + A_{c22} \Delta x_2 + A_{c23} [\Delta v_{2ref} \quad \Delta \omega_{2ref}] \quad (33)$$

Where

$\Delta x_{c2} = [\Delta i'_{12d}, \Delta i'_{12q}, \Delta i'_{2d}, \Delta i'_{2q}, \Delta v'_{2d}, \Delta v'_{2q}, \Delta i_{aa}, \Delta v_{aa}, \Delta i_{bb}, \Delta v_{bb}, \Delta \omega_2]$  with  $\Delta i_{aa}, \Delta v_{aa}, \Delta i_{bb}, \Delta v_{bb}$  as control variables. Assuming the reference values of  $\Delta v_{i2dref}$  and  $\Delta v_{i2qref}$  are tracked, (34) can be obtained.

$$\Delta v_{i2} = D_{21} \Delta x_{c2} + D_{22} [\Delta v_{2ref} \quad \Delta \omega_{2ref}] \quad (34)$$

Where

$$D_{21} = \begin{bmatrix} 0 & 0 & -k_{fm} v_{2d}^o & -k_{fm} v_{2q}^o & -k_{fm} i_{1d}^o & -k_{fm} i_{1q}^o & 0 & 0 & 0 & 0 & -k_{pcc} k_{im} \\ 0 & 0 & k_{fm} v_{2d}^o & -k_{fm} v_{2q}^o & -k_{fm} i_{1d}^o & -k_{fm} i_{1q}^o & 0 & 0 & 0 & 0 & k_{pcc} k_{im} \\ 0 & 0 & k_{fm} v_{2d}^o & -k_{fm} v_{2q}^o & -k_{fm} i_{1d}^o & -k_{fm} i_{1q}^o & 0 & 0 & 0 & 0 & k_{pcc} k_{im} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

$$D_{22} = \begin{bmatrix} 0 & k_{pcc} k_{im} \\ 0 & 0 \end{bmatrix}$$

Combining Fig.13 and (30)

$$\Delta \omega_2 = E_{21} \Delta x_{c2} + E_{22} [\Delta v_{2ref} \quad \Delta \omega_{2ref}] \quad (35)$$

Where

$$E_{21} = \begin{bmatrix} 0 & 0 & -\frac{1}{k_{fm}} v_{2d}^o & -\frac{1}{k_{fm}} v_{2q}^o & -\frac{1}{k_{fm}} i_{1d}^o & -\frac{1}{k_{fm}} i_{1q}^o & 0 & 0 & 0 & 0 \\ E_{22} = [0 \quad 1]. \end{bmatrix}$$

Then, (27) can be rewritten as

$$\dot{\Delta x}_2 = A A_2 \Delta x_2 + A B_2 \Delta x_{c2} + B B_2 [\Delta v_{2ref} \quad \Delta \omega_{2ref}] + B_3 \Delta v_{i2} \quad (36)$$

### c) Network Model

According to the equivalent MG network shown in Fig.3.9, it can be derived that

$$\begin{aligned} R_1 i^{i1} + L_1 \frac{di^{i1}}{dt} &= v^{vf} - v^{pcc} \\ R_2 i^{i2} + L_2 \frac{di^{i2}}{dt} &= v^{PQ} - v^{pcc} \\ R_3 i^{i3} + L_3 \frac{di^{i3}}{dt} &= v^{pcc} \\ C_p \frac{dv^{pcc}}{dt} &= i^{i1} + i^{i2} - i^{i3}. \end{aligned} \quad (37)$$

It can be rewritten in matrix as

$$\dot{\Delta x}_{net} = A_{net} \Delta x_{net} + B_{net}^{vf} \Delta v^{vf} + B_{net}^{PQ} \Delta v^{PQ} \quad (38)$$

$$\Delta x_{net} = [\Delta i_d^{i1} \quad \Delta i_q^{i1} \quad \Delta i_d^{i2} \quad \Delta i_q^{i2} \quad \Delta i_d^{i3} \quad \Delta i_q^{i3} \quad \Delta v_d^{pcc} \quad \Delta v_q^{pcc}]$$

$$\Delta v^{vf} = [\Delta v_d^{vf} \quad \Delta v_q^{vf}] \quad \Delta v^{PQ} = [\Delta v_d^{PQ} \quad \Delta v_q^{PQ}]$$

$(\Delta i_d^{i1}, \Delta i_q^{i1}), (\Delta i_d^{i2}, \Delta i_q^{i2}), (\Delta i_d^{i3}, \Delta i_q^{i3})$ , and  $(\Delta v_d^{pcc}, \Delta v_q^{pcc})$  are the  $d$ - $q$  components of  $L_1, L_2$  and  $L_3$  current and PCC voltage in the global frame,  $(v_d^{vf}, v_q^{vf})$  and  $(v_d^{PQ}, v_q^{PQ})$  the voltage of VFDC- based ESS and PQDC- based ESS in the global frame, respectively.

### d) Complete MG Model

Taking the reference frame of the VFDC-based ESS as the global reference of the MG system, all the other ESSs, loads, and network are transited to this global reference frame through the following transformation:

$$\Delta i^{PQ} = T_s \begin{bmatrix} 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \end{bmatrix} \Delta x_2 + T_C [\Delta \delta_2] \quad (39)$$

Where

$$T_s = \begin{bmatrix} \cos \delta_0 & -\sin \delta_0 \\ \sin \delta_0 & \cos \delta_0 \end{bmatrix} \quad T_C = \begin{bmatrix} -I_{2d}^0 \sin \delta_0 - I_{2q}^0 \cos \delta_0 \\ I_{2d}^0 \cos \delta_0 - I_{2q}^0 \sin \delta_0 \end{bmatrix}$$

And

$$[\Delta v_{b2}] = T_s^{-1} [\Delta v^{PQ}] + T_v [\Delta \delta_2] \quad (40)$$

Where

$$T_v = \begin{bmatrix} -v_d^{PQ0} \sin \delta_0 + v_q^{PQ0} \cos \delta_0 \\ -v_d^{PQ0} \cos \delta_0 - v_q^{PQ0} \sin \delta_0 \end{bmatrix}$$

$v_d^{PQ0}$  and  $v_q^{PQ0}$  are the steady – state value of  $v_d^{PQ}$  and  $v_q^{PQ}$ .

As to the VFDC-based ESS, the following conditions should be met in the global reference frame:

$$v^{vf} = R_4 (i^{vf} - i^{l1}) + L_4 \frac{d(i^{vf} - i^{l1})}{dt} \quad (41)$$

It can be rewritten as

$$\begin{aligned} \Delta v^{vf} = & \begin{bmatrix} -R_4 & L_4 \omega_e \\ -L_4 \omega_e & -R_4 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix} \Delta x_{net} \\ & + \begin{bmatrix} -L_4 & 0 \\ 0 & -L_4 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix} \Delta \dot{x}_{net} \\ & + \begin{bmatrix} R_4 & -L_4 \omega_e \\ \omega_e L_4 & R_4 \end{bmatrix} \begin{bmatrix} 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \end{bmatrix} \Delta x_1 \\ & + \begin{bmatrix} L_4 & 0 \\ 0 & L_4 \end{bmatrix} \begin{bmatrix} 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \end{bmatrix} \Delta \dot{x}_1 \end{aligned} \quad (42)$$

Similarly, as to the PQDC-based ESS, the following conditions should be met in the global reference frame:

$$v^{PQ} = \frac{d(i^{PQ} - i^{l2})}{dt} L_5 + (i^{PQ} - i^{l2}) R_5 \quad (43)$$

It can be rewritten as

$$\Delta v^{PQ} = E_{21} \Delta x_{net} + E_{22} \Delta \dot{x}_{net} + D_{21} \Delta i^{PQ} + D_{22} \Delta \dot{i}^{PQ} \quad (44)$$

Where

$$\begin{aligned} E_{21} = & \begin{bmatrix} -R_5 & L_5 \omega_e \\ -L_5 \omega_e & -R_5 \end{bmatrix} \begin{bmatrix} 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \end{bmatrix} \\ E_{22} = & \begin{bmatrix} -L_5 & 0 \\ 0 & -L_5 \end{bmatrix} \begin{bmatrix} 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \end{bmatrix} \\ D_{21} = & \begin{bmatrix} R_5 & -L_5 \omega_e \\ L_5 \omega_e & R_5 \end{bmatrix} \\ D_{22} = & \begin{bmatrix} L_5 & 0 \\ 0 & L_5 \end{bmatrix} \end{aligned}$$

Therefore, the MG global small-signal model can be derived

$$\begin{bmatrix} \Delta \dot{x}_1 \\ \Delta \dot{x}_{c1} \\ \Delta x_2 \\ \Delta \dot{x}_{c2} \\ \Delta x_{net} \end{bmatrix} = [A] \begin{bmatrix} \Delta x_1 \\ \Delta x_{c1} \\ \Delta x_2 \\ \Delta x_{c2} \\ \Delta x_{net} \end{bmatrix} + [B] \begin{bmatrix} \Delta v_{1ref} \\ \Delta \omega_{1ref} \\ \Delta v_{2ref} \\ \Delta \omega_{2ref} \end{bmatrix} \quad (45)$$

## V. BLDC MOTOR

High efficiency, high power density and wide range speed controllability of BLDC motors make them suitable in various drive applications. In particular the spindle motors used in computer hard disk drives are to possess high speed characteristics for fast data access.

Brushless Direct Current (BLDC) motors are one of the motor types rapidly gaining popularity. BLDC motors are used in industries such as Appliances, Automotive, Aerospace, Consumer, Medical, Industrial Automation equipment and Instrumentation. As the name implies, BLDC motors do not use brushes for commutation; instead, they are electronically commutated. BLDC motors have many advantages over brushed DC motors and induction motors. A few of these are:

- Better speed versus torque characteristics
- High dynamic response
- High efficiency
- Long operating life
- Noiseless operation
- Higher speed ranges

In addition, the ratio of torque delivered to the size of the motor is higher, making it useful in

applications where space and weight are critical factors. In this application note, we will discuss in detail the construction, working principle, characteristics and typical applications of BLDC motors.

## A) Main Characteristics BLDC Motor

Brushless DC motors consist of two coaxial magnetic armatures separated by an air gap. In certain types of motor,

- The external armature, the stator, is fixed.
- The internal armature, the rotor, is mobile (the rotor can also be external in certain cases).
- The stator is the induced part of the machine.
- The rotor is the inductor of the machine.
- In brushless DC motors, the internal armature, the rotor, is a permanent magnet. This armature is supplied by a constant current (DC).
- The external armature (stator) is poly phased (3 phases in our case) and is covered by poly- phased currents.

In a Brushless DC motor, the rotor is a permanent magnet, this type of motor has almost the same properties and physical laws as a DC current machine.

An electric motor transforms electrical energy into mechanical energy. Two main characteristics of a brushless DC motor are:

- It has an electromotive force proportional to its speed
- The stator flux is synchronized with the permanent magnet rotor flux.

## VI. MATLAB/SIMULATION RESULTS

### Case 1: PQ Control with fixed load

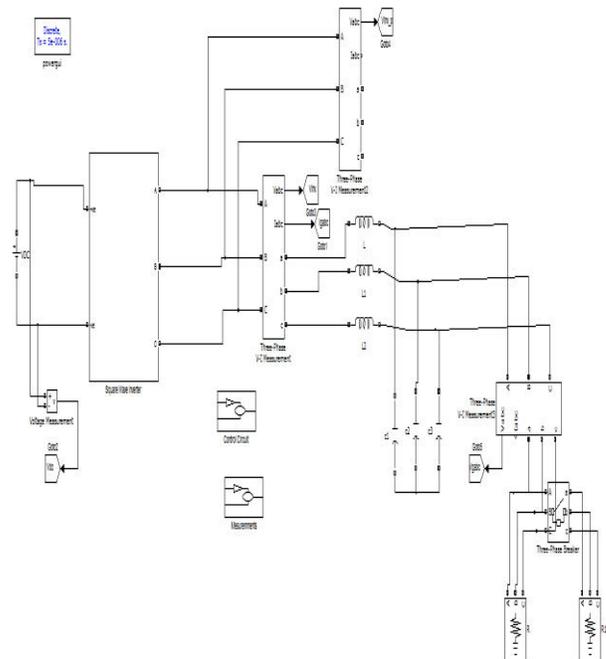


Fig.14 Matlab/Simulink model of PQ control with fixed load

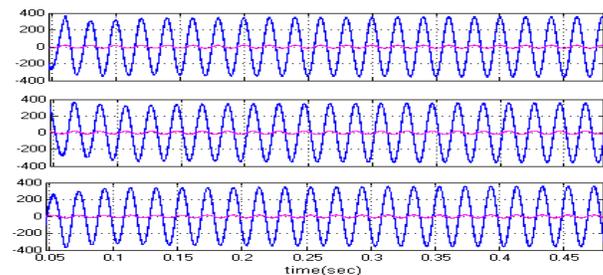


Fig.15 Steady-state voltage and current curves

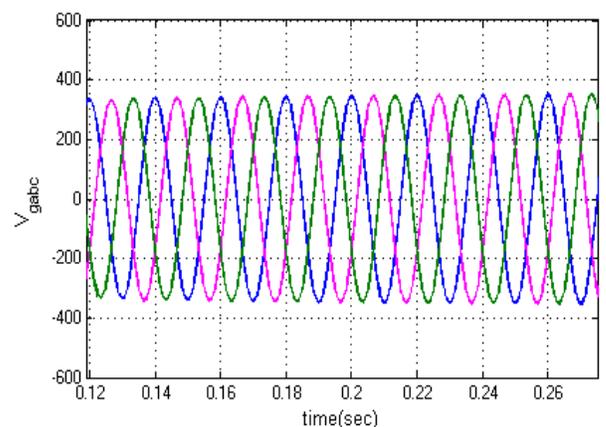


Fig.16 Source Voltages (V)

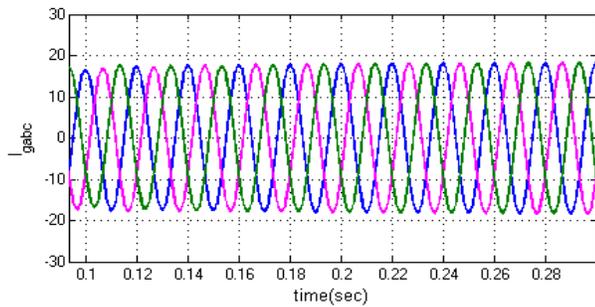


Fig.17 Source Currents (A)

**Case: 2 PQ Control variable Decremental load**

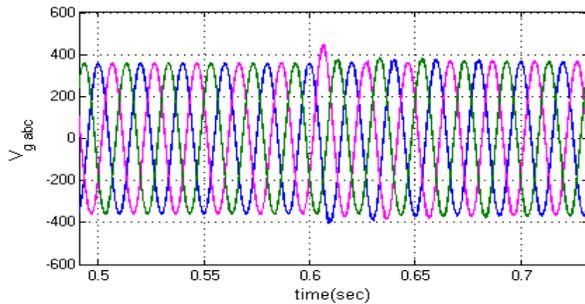


Fig.18 Source Voltages (V)

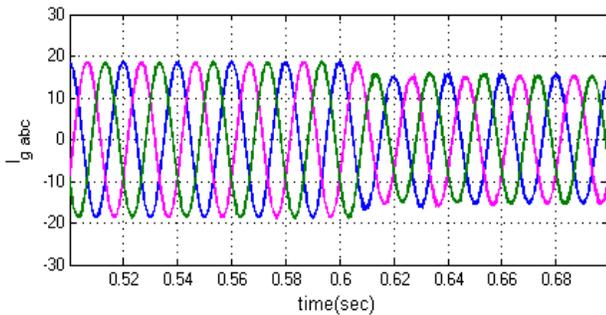


Fig.19 Source Currents (A)

**Case: 3 PQ Control variable Incremental load**

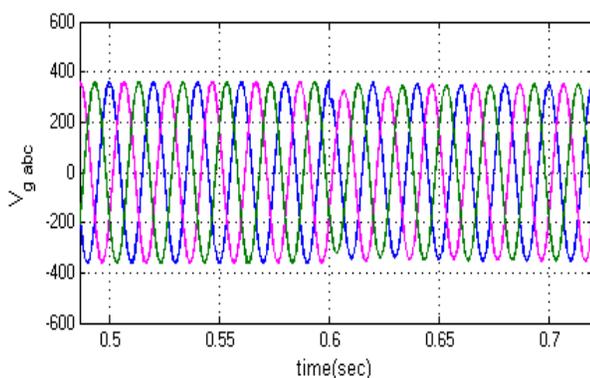


Fig.20 Source Voltages (V)

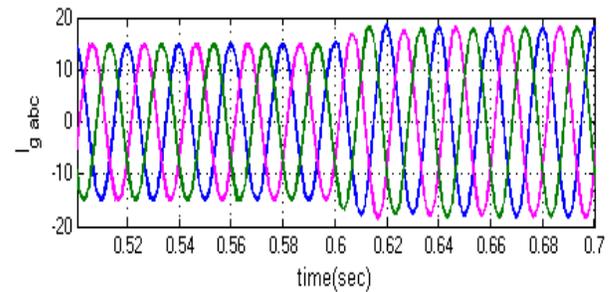


Fig.21 Source Currents (A)

**Case: 4 VF control Fixed load**

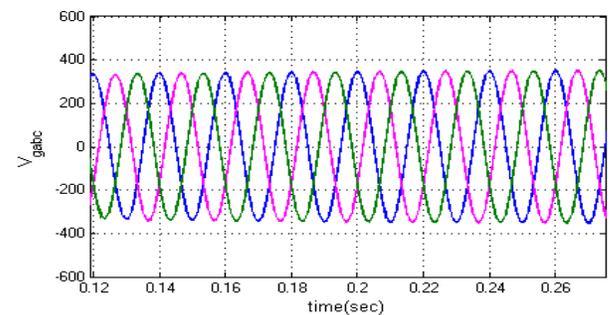


Fig.22 Source Voltages (V)

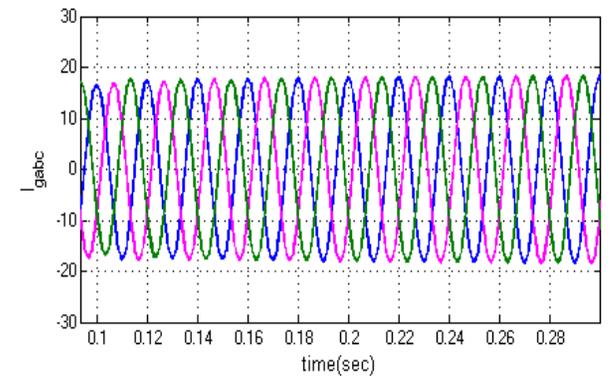


Fig.23 Source Currents (A)

**Case: 5 VF control variable with Decremental load**

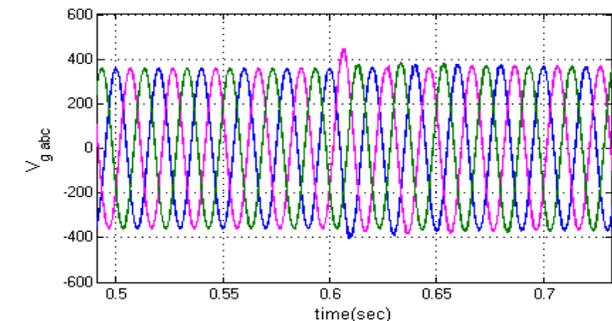


Fig.24 Source Voltages (V)

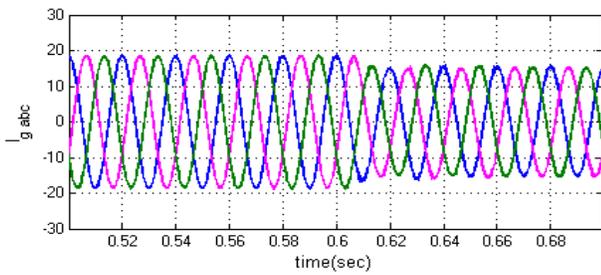


Fig.25 Source Currents (A)

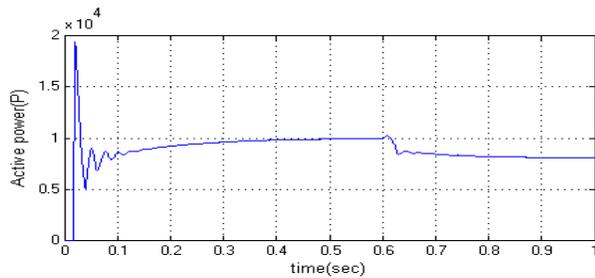


Fig.26 Active Power (P)

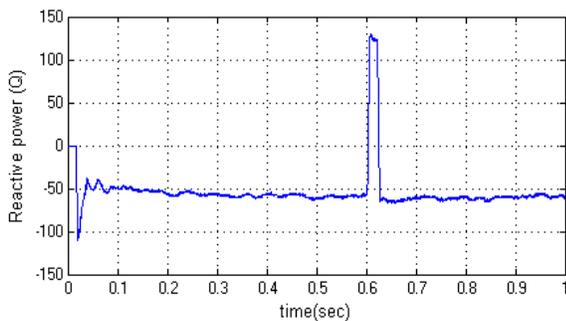


Fig.27 Reactive Power (Q)

**Case: 6 VF control variable with Incremental load**

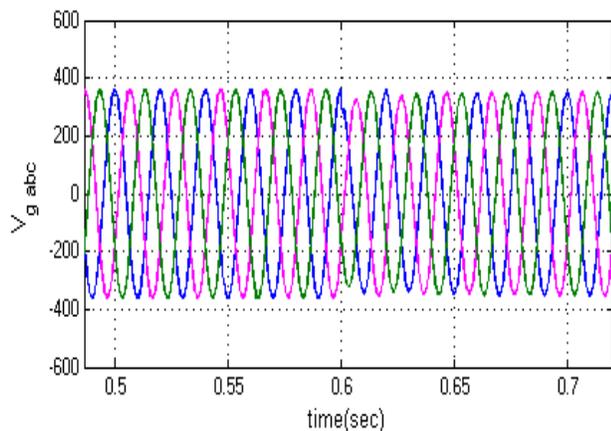


Fig.28 Source Voltages (V)

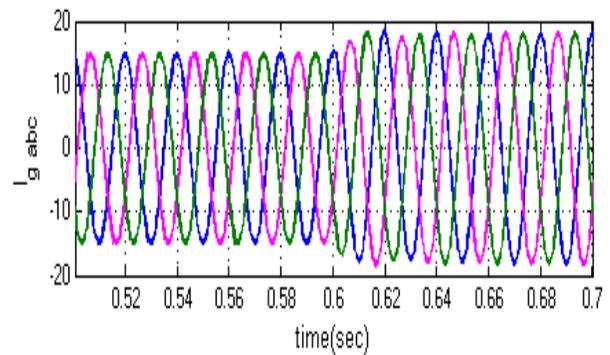


Fig.29 Source Currents (A)

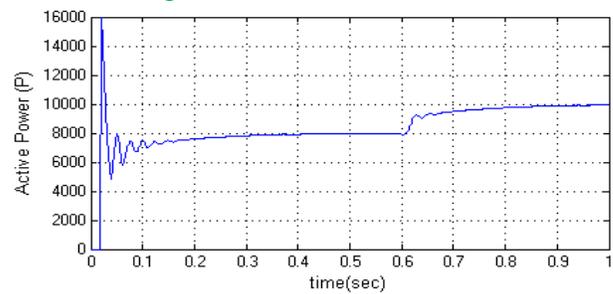


Fig.30 Active Power (P)

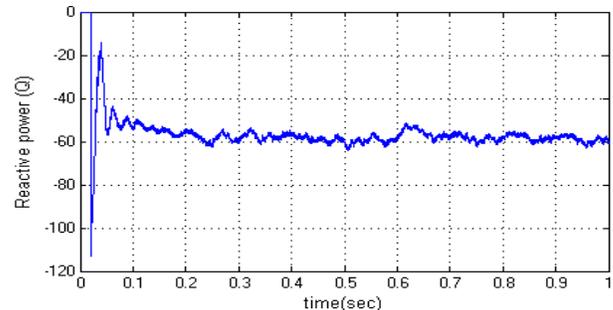


Fig.31 Reactive Power (Q)

**Case: 7 PQ control fixed load with BLDC Motor**

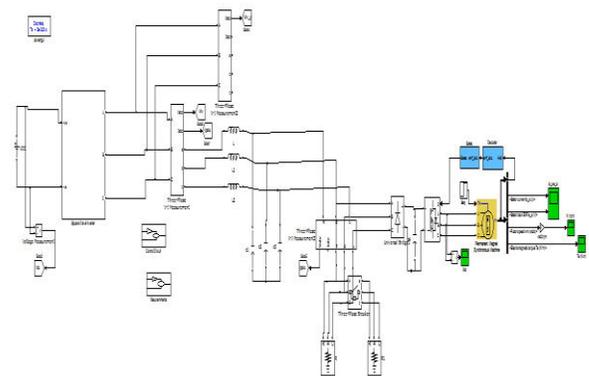


Fig.32 Matlab/Simulink model of BLDC motor with fixed load

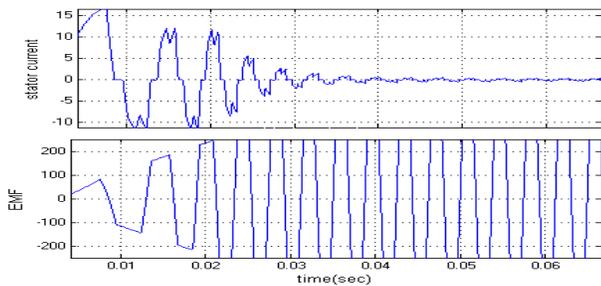


Fig.33 Stator Current (A) and EMF of the BLDC motor

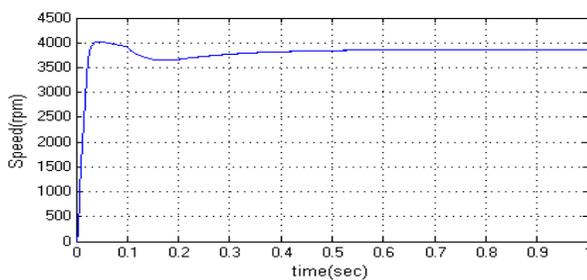


Fig.34 Speed Curve of the BLDC motor

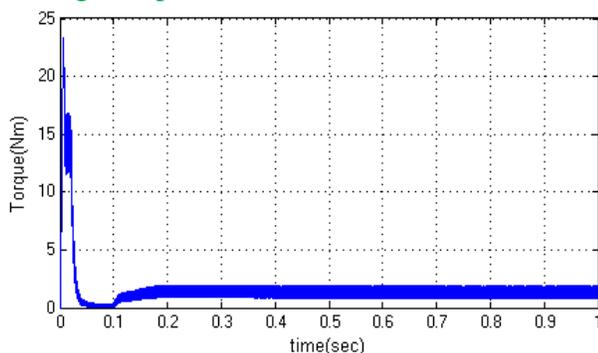


Fig.35 Torque Characteristics of the BLDC Motor

## VII. CONCLUSION

In this paper proposes a voltage and frequency is controlled by energy storage system. For this purpose, a droop control strategy is used as follows. For the verification of the correct operation of the energy storage system, several different scenarios, including the disconnection of the microgrid from the main grid and the constant variation of the load in the islanding mode, are designed. Characteristics of a BLDC motor as a sample load was observed by Matlab simulation results. It was concluded that both

the duration and intensity of the fault can determine how the frequencies of different DGs in the microgrid will be stabilized.

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